A method for simultaneously counterbalancing condition order and assignment of stimulus materials to conditions

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Abstract Counterbalanced designs are frequently used in the behavioral sciences. Studies often counterbalance either the order in which conditions are presented in the experiment or the assignment of stimulus materials to conditions. Occasionally, researchers need to simultaneously counterbalance both condition order and stimulus assignment to conditions. Lewis (1989; Behavior Research Methods, Instruments, & Computers 25:414-415, 1993) presented a method for constructing Latin squares that fulfill these requirements. The resulting Latin squares counterbalance immediate sequential effects, but not remote sequential effects. Here, we present a new method for generating Latin squares that simultaneously counterbalance both immediate and remote sequential effects and assignment of stimuli to conditions. An Appendix is provided to facilitate implementation of these Latin square designs.

Keywords Counterbalancing · Latin square · Order effects · Sequential effects · Experimental design

Researchers from such diverse fields as cognitive psychology, neuroscience, political science, clinical science, movement science, and human factors research frequently counterbalance condition order to prevent the effects of general practice, fatigue, or other unwanted order effects from causing differences between conditions. Counterbalancing is generally achieved by creating Latin squares. Table 1 shows a Latin square that counterbalances condition order. In the Latin square, each condition (represented by a letter) occurs once in each row (i.e., for each participant) and once in each column

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In this article, we discuss methods that counterbalance sequential effects in addition to ordinal position. Sequential effects occur when performance in a condition is affected by the condition(s) preceding it. For example, a particularly difficult condition may induce a negative affective state that lingers for some time and negatively influences performance in the condition presented after it. If the same conditions follow each other for each participant (e.g., condition B always follows condition A), comparisons of performance in the different conditions may be tainted. Imagine, for example, that one uses the Latin square shown in Table 1 and that condition A exerts a negative influence on performance in the condition immediately following it. Because condition B always follows condition A, performance in condition B will be underestimated relative to the other conditions (i.e., C, D, E, and F). Performance in a condition can be affected by a condition immediately preceding it (i.e., an immediate sequential effect) or by a condition preceding it by two or more positions in the sequence of conditions (i.e., a remote sequential effect). Studies have shown that immediate and remote sequential effects do, in fact, occur and affect diverse dependent variables such as category judgments (Petzold & Haubensak, 2001), memory judgments (Malmberg & Annis, 2012), absolute identification (Stewart, Brown, & Chater, 2005), skill acquisition (Matlen, & Klahr, 2013), questionnaire-based measurements of shame (Faulkner & Cogan, 1990), and the taste of food and wine (Durier, Monod, & Bruetschy, 1997; Schlich, 1993). Such widespread findings of sequential effects indicate that it is safer to control for sequential effects than to simply assume (or hope) that sequential effects won't affect the results. Thus, rather than

Table 1 Example of a Latin square design with six conditions

Participant	Condition Order
1,7,	ABCDEF
2, 8,	BCDEFA
3, 9,	CDEFAB
4,10,	DEFABC
5, 11,	EFABCD
6, 12,	FABCDE

Note. Capital letters represent conditions. In a typical counterbalanced design, each participant receives one condition order, and an equal number of participants are tested with each condition order

using a type of Latin square such as the one shown in Table 1, which counterbalances ordinal position, but not sequential effects, we recommend using Latin squares that counterbalance sequential effects in addition to ordinal position.

Several methods have been developed for counterbalancing immediate sequential effects in addition to ordinal position (Bradley, 1958; Wagenaar, 1969; Williams, 1949). The Latin square in Table 2 is constructed according to a method proposed by Bradley. In this method, the top row of the square is constructed as A, N, B, N-1, C, N-2, and so on, where N is the total number of conditions. Subsequent rows are created by putting the next letter in the alphabetical sequence below each letter of the preceding row. An important property of the Latin square in Table 2 is that across participants, no condition is preceded (and followed) more than once by another condition, a property that has been referred to as "digram-balanced" (Wagenaar, 1969). Note that the Latin square shown in Table 2 counterbalances immediate sequential effects, but not remote sequential effects. Latin squares that counterbalance remote sequential effects exist for some situations and are discussed later. Latin squares are often discussed in the context of counterbalancing order effects but are also used to counterbalance the assignment of stimulus materials to conditions. Counterbalancing stimulus assignment to conditions eliminates confounds in item difficulty between the different

 Table 2 Example of digram-balanced Latin square designs with six conditions

Condition Order		
AFBECD		
BACFDE		
CBDAEF		
DCEBFA		
EDFCAB		
FEADBC		

conditions of the experiment (e.g., Pollatsek & Well, 1995) and plays an important role in the design of many behavioral experiments.

In some experiments, both the condition order and assignment of stimulus materials to conditions need to be counterbalanced. For example, de Jonge, Tabbers, Pecher, and Zeelenberg (2012) studied the effect of presentation rate on paired-associate learning. Word pairs (e.g., hammer-elevator) were presented for a total study time of 16 s in five blocks with different presentation rates (i.e., 16×1 s, 8×2 s, 4×4 s, 2×8 s, and 1×16 s). Presentation rate was blocked so that within each block the presentation rate was constant. After study, one word of each pair (e.g., hammer-?) was presented in a cued recall test, and participants had to report the corresponding target word (e.g., elevator). To sensibly compare performance under different presentation rate conditions, the order of conditions (blocks) needs to be counterbalanced. Moreover, for obvious reasons, a single participant cannot study the same word pair in each of the five conditions. The stimuli must therefore be divided into separate stimulus sets that are assigned to the different presentation rate conditions. Because word pairs differ in how easy they are to learn (e.g., Nelson & Dunlosky, 1994), the assignment of stimulus materials to conditions also needs to be counterbalanced (i.e., in addition to condition order). A combination of all possible condition orders and all possible stimulus assignments to conditions results in $n! \times n!$ permutations (giving 14,400 permutations for an experiment with five conditions). As a result, in all but the simplest designs, using all possible permutations is practically impossible.

A more useful approach to this problem is to use a Latin square design that counterbalances both condition order and assignment of stimuli to conditions. A solution to this problem is provided by Lewis (1989, 1993). Since the method is somewhat easier for experiments with an odd number of conditions, we describe that situation first. In the first step, a pair of Latin squares representing the conditions is created using Bradley's (1958) method (where the second square is the vertically mirrored version of the first square). In the second step, a pair of Latin squares representing the stimulus sets is created. This second pair of Latin squares is a copy of the first pair, except that numbers are used in the second pair of Latin squares. The numbers in the second set of Latin squares correspond to the letters of the first set of Latin squares such that the letter A becomes the number 1, the letter B becomes number 2, and so forth (compare the adjacent letter and number matrices, shown below). In the third step, these Latin squares are combined in a diagonal fashion (i.e., the first square of letters is combined with the second square of numbers and vice versa), to create two Latin squares that counterbalance condition order and the assignment of stimulus materials to conditions. The resulting Latin squares are shown in Table 3.

B Z C I D (E B A C B D C E D A	E A B	D E A	\times	1 2 3 4 5	1 2 3	3 4 5	4 5 1 2 3	4 5 1	
D I E Z A I	DB EC AD BE CA	A B C	B C D		4 5 1	1	3 4 5	1 2 3	2 3	

The procedure is different for Latin squares with an even number of conditions. In the first step, a pair of Latin squares representing the conditions is created. The first Latin square is again created using Bradley's (1958) method. The second Latin square representing conditions is created by swapping each pair of adjacent columns (e.g., columns 1 and 2, columns 3 and 4, etc.) of the first Latin square. In the second step, a pair of Latin squares representing stimulus sets is created. The first Latin square for stimulus sets is a copy of the first Latin square for conditions where the letters have been replaced by corresponding numbers (i.e., $A \rightarrow 1, B \rightarrow 2$, etc.). The second Latin square for stimulus sets is created by copying the second Latin square for conditions in a similar fashion, but an additional transformation is needed. The rows of this Latin square are rotated by one position (i.e., row 1 of this Latin square becomes row 8, row 2 becomes row 1, row 3 becomes row 2, etc.). The resulting matrices are shown below. In

 Table 3
 A pair of Latin squares that counterbalances condition order and the assignment of stimulus materials to conditions

	ЦЭ D0
A3 E4 B2 D5 C1	F6 E7
B4 A5 C3 E1 D2	G7 F8
C5 B1 D4 A2 E3	H8 G1
D1 C2 E5 B3 A4	
E2 D3 A1 C4 B5	H1 A8
	A2 B1
C1 D5 B2 E4 A3	B3 C2
D2 E1 C3 A5 B4	C4 D3
E3 A2 D4 B1 C5	D5 E4
A4 B3 E5 C2 D1	E6 F5
B5 C4 A1 D3 E2	F7 G6
	C0 117

Note. Capital letters represent conditions; numbers represent stimulus sets

the third step, these Latin squares are combined in a diagonal fashion (just as before). See Table 4 for the resulting pair of Latin squares.

A H B A C B D C E D F E G F H G	C D E F G H	G H A B C D E F	C D E F G H A B	F G H A B C D E	D F G H A B C	E F G H A B C D	\times	1 2 3 4 5 6 7 8	8 1 2 3 4 5 6 7	2 3 4 5 6 7 8 1	7 8 1 2 3 4 5 6	3 4 5 6 7 8 1 2	6 7 8 1 2 3 4 5	4 5 6 7 8 1 2 3	5 7 8 1 2 3 4
H A B C C D C E F G G H	H A C D E	B C D E F G H A	F G H A B C D E	C D E F G H A B	E F G H A B C D	D F G H A B C		1 2 3 4 5 6 7 8	2 3 4 5 6 7 8 1	8 1 3 4 5 6 7	3 4 5 6 7 8 1 2	7 8 1 2 3 4 5 6	4 5 7 8 1 2 3	6 7 8 1 2 3 4 5	5 7 8 1 2 3 4

The method proposed by Lewis (1989) counterbalances condition order and the assignment of stimulus materials to conditions for digram-balanced Latin squares constructed with Bradley's method. Bradley (1958) pointed out, however, that this procedure counterbalances immediate sequential effects, but not remote sequential effects. For example, in the Latin square shown in Table 2, condition E is twice preceded by condition F in the second cell preceding it (see rows 1 and 2 of the Latin square). To solve this problem, Alimena (1962)

 Table 4
 A pair of Latin squares that counterbalances condition order and the assignment of stimulus materials to conditions

A1	H2	B8	G3	C7	F4	D6	E5	
В2	A3	C1	H4	D8	G5	E7	F6	
CЗ	Β4	D2	A5	E1	H6	F8	G7	
D4	C5	ЕЗ	Bб	F2	A7	G1	H8	
E5	D6	F4	C7	G3	В8	H2	A1	
F6	E7	G5	D8	H4	C1	A3	В2	
G7	F8	НG	E1	A5	D2	B4	C3	
H8	G1	A7	F2	Bб	ЕЗ	C5	D4	
H1	A8	G2	В7	F3	C6	E4	D5	
A2	В1	НЗ	C8	G4	D7	F5	ЕG	
BЗ	C2	A4	D1	H5	E8	G6	F7	
C4	D3	В5	E2	A6	F1	H7	G8	
D5	E4	C6	FЗ	В7	G2	A8	H1	
E6	F5	D7	G4	C8	HЗ	В1	A2	
F7	G6	E8	H5	D1	A4	C2	BЗ	
G8	H7	F1	A6	E2	В5	D3	C4	

developed a method for constructing Latin squares that counterbalances immediate and remote sequential effects.

The method for constructing these Latin squares is somewhat complicated and perhaps best illustrated for a 10×10 Latin square. The first step in constructing this type of Latin square is to fill the first column by inserting the letters representing the conditions in ascending order. Subsequently, fill the last column by inserting the letters in descending order. Third, fill the cells on the diagonals with the letters that they connect (A to A and J to J in the example below). This results in the following partially filled matrix.

А									J
В	А							J	Ι
С		А					J		Н
D			А			J			G
Е				А	J				F
F				J	А				Е
G			J			А			D
Η		J					А		С
Ι	J							А	В
J									А

In the next step, the columns are filled by inserting letters in ascending order starting at the A in each column that is not yet completely filled. In the first partially filled column, insert the letter B by skipping one row (in the matrix below, see the column with number 1 above it). Then insert the letter C in this column, again skipping one row, and so on for all letters. The second partially filled column is filled by inserting the letter B skipping two rows below the letter A. The letter C is then inserted by again skipping two rows. Working your way through the matrix from left to right, each time you shift to the next right column, the number of rows skipped increases by 1 (the numbers above the columns indicate the number of rows that need to be skipped before inserting the next letter).

0 1 2 3 4 5 6 7 8 9	0	1 2	3 4	15	6	7	8	9
---------------------	---	-----	-----	----	---	---	---	---

А									J
В	А							J	Ι
С		А					J		Η
D	В		А			J			G
Е				А	J				F
F	С	В		J	А				Ε
~									
G			J			А			D
G H	D	J	-			A	A		D C
Η	D J		-			A	A	A	
H I			-	В		A	A	A	С

Whenever the bottom of the column is reached, continue from the top of the column, but skip one row less than you normally would for that column. For example, for the column with the number 1 above it, the letter F is inserted on the first row. The easiest way to implement this rule is to include the row with numbers above the matrix in the count of the number of rows that are skipped. After continuing from the top of the column, insert the other letters by skipping the appropriate number of rows for that column (e.g., in the column with the number 2 above it, the letter E is inserted by skipping two rows). Depending on the column, you will need to cycle through this procedure several times before the column is completely filled. The matrix below shows an intermediate result in which we started once from the top of the matrix for each column.

A	F	D	С		В				J
В	А							J	Ι
С	G	А				В	J		Η
D	В	Е	А	С		J			G
Ε	Η		D	А	J		В		F
F	С	В		J	А				Ε
G	Ι	F	J			А		В	D
Η	D	J	В				А		С
Ι	J	С	Ε					А	В
J	Ε	G		В					А

0 1 2 3 4 5 6 7 8 9

Table 5 presents the completely filled matrix (i.e., the 10×10 Latin square). As was noted by Alimena (1962), this method works only when n + 1 is a prime number (where n is the number of conditions). Thus, this method can be used to construct Latin squares for experiments with 2, 4, 6, 10, 12, 16, 18, 22, 28, . . . conditions.

As was mentioned, the method proposed by Lewis (1989) counterbalances condition order and the assignment of stimulus materials to conditions, but this method controls only for immediate sequential effects. To the best of our knowledge, no such method has been published for designs that control for both immediate and remote sequential effects. We therefore set out to find a method that counterbalances condition order and assignment of stimulus materials to conditions for Latin squares that control for both immediate and remote sequential effects. The following method provides a solution. Like the method proposed by Lewis (1989), this method requires constructing a

 Table 5
 Example of a Latin square with ten conditions that controls for both immediate and remote sequential effects

	-
AFDCIBHGEJ	
BAHFGDECJI	
CGAIEFBJDH	
DBEACHJFIG	
EHIDAJGBCF	
FCBGJADIHE	
GIFJHCAEBD	
HDJBFEIAGC	
IJCEDGFHAB	
JEGHBICDFA	

pair of Latin squares. The first step involves creating a pair of Latin squares representing conditions. The first Latin square representing conditions is constructed using the method of Alimena (1962). The second Latin square representing conditions is constructed by mirroring the first square. Note that the first square can be mirrored along either the vertical axis or the horizontal axis, since this gives the same result. Below is an example for an experiment with six conditions.

А	D	Е	В	С	F
В	А	С	D	F	Е
С	Ε	А	F	В	D
D	В	F	А	Е	С
Е	F	D	С	А	В
F	С	В	Ε	D	А
F	С	В	Е	D	A
F E	C F				A B
Ε	F	D	С	А	В
E D	F B	D F	C A	A E	B C

The construction of the Latin squares representing stimulus sets is somewhat complicated and involves several operations. First, copy the first Latin square for conditions and replace the letters with their corresponding numbers (i.e., $A \rightarrow 1$, $B \rightarrow 2$, etc.). This results in the following Latin square:

1	4	5	2	3		
2	1	3	4	6	5	
3	5	1	62		4	
					-	
4	2	6	1	5	3	
				5 1		

Next, two Latin squares representing stimulus sets need to be created. The first Latin square is created by separately mirroring the top and bottom halves of the original Latin square along an imaginary horizontal line running through the center of the matrix. For a 6×6 Latin square, this causes rows 1 and 3 to be swapped, as well as rows 4 and 6, resulting in the following Latin square:

3	5	1	6	2	4
2	1	3	4	6	5
1	4	5	2	3	6
6	3	2	5	4	1
5	6	4	3	1	2
4	2	6	1	5	3

The second Latin square is created by swapping the adjacent rows of numbers from the original number Latin square but leaving the top and bottom rows untouched. Thus, for a 6×6 Latin square, rows 3 and 2 are swapped, and rows 4 and 5 are swapped, resulting in the following Latin square:

				3	
3	5	1	6	2	4
2	1	3	4	6	5
				1	
1	2	6	1	5	3
5	3	2	5	4	1

Next, the Latin squares representing conditions and the Latin squares representing stimulus sets need to be combined to construct a pair of Latin squares. It turns out that the two Latin squares representing conditions and the two Latin squares representing stimulus sets can be paired either way, as long as each Latin square is used only once. Both possible pairings result in a pair of Latin squares counterbalancing condition order and assignment of stimulus materials to conditions, while controlling for both immediate and remote sequential effects. One of the two possible pairings is shown in Table 6.

We have no formal proof that this method works for Latin squares of all sizes but have successfully tried it for Latin squares up to size 16×16 , a number that seems large enough for all but the most ambitious experiments.

Concluding remarks and recommendations

In this article, we have discussed methods that counterbalance sequential effects in addition to ordinal position. As has been shown, the methods of Bradley (1958) and Alimena (1962) can be extended to simultaneously counterbalance sequential effects and the assignment of stimulus materials to conditions. We recommend that researchers use counterbalancing methods that maximize control over sequential effects. More specifically, for studies that require simultaneous counterbalancing of

 Table 6
 A pair of Latin squares that counterbalance condition order and the assignment of stimulus materials to conditions and control for both immediate and remote sequential effects

A1 D4 E5 B2 C3 F6
B3 A5 C1 D6 F2 E4
C2 E1 A3 F4 B6 D5
D5 B6 F4 A3 E1 C2
E4 F2 D6 C1 A5 B3
F6 C3 B2 E5 D4 A1
F3 C5 B1 E6 D2 A4
E2 F1 D3 C4 A6 B5
D1 B4 F5 A2 E3 C6
C6 E3 A2 F5 B4 D1
B5 A6 C4 D3 F1 E2
A4 D2 E6 B1 C5 F3

Note. Capital letters represent conditions; numbers represent stimulus sets

condition order and stimulus assignment to conditions, we recommend the following.

- Whenever possible, use the method developed in the present article to create Latin squares that simultaneously counterbalance condition order and stimulus assignment to conditions. These Latin squares control for both immediate and remote sequential effects. Note that this method can be used only when the number of conditions + 1 is a prime number (i.e., for experiments with 2, 4, 6, 10, 12, . . . conditions).
- 2. If the method developed in the present article cannot be used, use the method proposed by Lewis (1989).

Appendix

2 conditions

Pairs of Latin squares that simultaneously counterbalance the order of conditions and the assignment of stimulus materials to conditions

A1 B2 B2 A1 B1 A2 A2 B1 4 conditions A1 C3 B2 D4 B3 A4 D1 C2 C2 D1 A4 B3 D4 B2 C3 A1 D2 B1 C4 A3 C1 D3 A2 B4 B4 A2 D3 C1 A3 C4 B1 D2 6 conditions D4 E5 B2 C3 F6 Α1 B3 A5 C1 D6 F2 E4 C2 E1 A3 F4 B6 D5 D5 B6 F4 A3 E1 C2 E4 F2 D6 C1 A5 B3 F6 C3 B2 E5 D4 A1 F3 C5 B1 E6 D2 A4 E2 F1 D3 C4 A6 B5 D1 B4 F5 A2 E3 C6 C6 E3 A2 F5 B4 D1 B5 A6 C4 D3 F1 E2 A4 D2 E6 B1 C5 F3 10 conditions G7 Α1 F6 D4 C3 Ι9 В2 Н8 E5 A7 Н1 F9 G5 D6 E2 C10 J4 В3 C2 G1 Α8 Ι6 E7 F4 В5 JЗ D10 D5 B8 E9 C1J7 F2 A4 H10 Т.3 Ε4 H2 Ι5 D1 AЗ J8 G10 В6 С9 F7 С9 В6 G10 J8 AЗ D1 Ι5 H2 G6 ΤЗ F2 H10 C1 Α4 E.9 B8 .17 H9 D10 J3 В5 F4 E7 I6 Α8 G1 Ι8 J4 C10 E2 D6 G5 F9 H1 A7 G7 В2 Ι9 J10 E5 C3 F6 Н8 D4

Note that either method of simultaneously counterbalancing the order of conditions and assignment of stimuli to conditions requires a pair of Latin squares (regardless of the number of conditions). The methods for generating these Latin squares are somewhat complicated, but the Appendix should make implementation easy. The Appendix presents pairs of Latin squares for experiments with 2, 4, 6, 10, and 12 conditions that were created with the method proposed here. Lewis (1989) presents Latin squares that can be used for experiments with 3, 5, 7, or 8 conditions.

I10 C7 D2

FЗ

Α6

J.5

J10

Ι8

Н9

G6

F7

 ${\rm E}\,4$

D5

C2

В3

Α1

E8 G9 H4

В1

J5 I4 H3 G2 F1 E10	E8 J2 D7 I1 C6 H5	G9 C5 J1 F8 B4 I7	H4 E1 B9 J6 G3 D8	B1 D3 F5 H7 J9 A2	G8 E6 C4 A2 J9	F10 I2 A5 D8 G3	D2 H6 A10 E3 I7 B4	F3 A9 G4 B10 H5 C6	A6 B7 C8 D9 E10 F1			
D9	B10	E3	A5	C4	Н7	д5 Јб	F8	I1	G2			
C8	G4	A10	I2	E6	F5	в9	J1	D7	НЗ			
в7	A9	H6	F10		D3	E1	C5	J2	I4			
A6	F3	D2	C7	I10		H4	G9	E8	J5			
12	12 conditions											
A1	G7	Ι9	J10	H8	K11	в2	E5	C3	D4	F6	L12	
BЗ	A8	E1	G4	C11	Ι7	D6	J2	F9	H12	L5	K10	
C2	H1	Α5	D7	KЗ	G9	F4	B10	I6	L8	E12	J11	
D5	В9	J6	A11		EЗ	H10	G12	L2	C7		Ι8	
Ε4	I2	F10		A6	С5	J8	L7		G3			
F7	C10	B11		Ι4	A12	L1	D9	E8	K2	J3	G6	
G6	J3	K2	E8	D9	L1	A12	I4	H5				
H9 T0	D11	G3	B12	L7	J8	C5	A6	K1	F10		E4	
I8 T1 1	K4 E12	C7	L2	G12	H10 F4	E3	F1 K2		J6 DE		D5 C2	
J11 K10		L8 H12	I6 F9	B10 J2	гч D6	G9 I7	K3 C11	D7 G4	А5 Е1	H1 A8	B3	
L12		D4	C3	E5	B2	к11	H8	J10	I9	G7	A1	
L6	F3	D2	C8	E9	В1		H4	J5	I11			
K5	L9	H6	F11		D3		C12		E7			
J4 T2	E2	L10	I1	B6	F5	G8	K7		A3	H11		
I3	K8	C1	L4 D7	G11 L3		E6	F2	A9 KC			D10 E11	
H2 G1	D1 J7	G5 K9	В7 Е10	ЦЗ D8	J9 L11	C4 A2	AIU I5	К6 НЗ	F8 B4	112 C6		
F12		B4	H3	15	A2	A2 L11	D8	п3 E10		J7	г 12 G1	
E11		F8	K6	A10		J9	L3	B7		D1	H2	
D10		J12		F2	E6	H7		L4	C1	K8	I3	
C9		A3	D12	K7	G8	F5	B6	I1	L10		J4	
В8	A4	E7	G2	C12	I10	D3	J1	F11		L9	K5	
A7	G10	I11	J5	H4	K12	В1	E9	С8	D2	FЗ	L6	

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